

Inference at \* 2  
of proof for Lemma before\_last:

1.  $T : \text{Type}$
2.  $T \text{ List}$
3.  $u : T$
4.  $v : T \text{ List}$
5.  $\forall x:T. (x \in v) \Rightarrow (\neg(x = \text{last}(v))) \Rightarrow x \text{ before last}(v) \in v$   
 $\vdash \forall x:T. (x \in [u / v]) \Rightarrow (\neg(x = \text{last}([u / v]))) \Rightarrow x \text{ before last}([u / v]) \in [u / v]$   
by InteriorProof ((((((((((Unfold 'l\_before' 0  
CollapseTHEN (
                    RWO "cons\_sublist\_cons" 0))·)
CollapseTHENM (RWO "cons\_member" 0))·)
CollapseTHEN ((Auto\_aux (first\_nat 1:n) ((first\_nat 1:n),(first\_nat
  3:n)) (first\_tok :t) inil\_term)))·)
CollapseTHEN (Reduce 0))·)
                    CollapseTHEN (SimpConcl))·

1:

6.  $x : T$
7.  $(x = u) \vee (x \in v)$
8.  $\neg(x = \text{last}([u / v]))$   
 $\vdash (x = u \ \& \ [\text{last}([u / v])] \subseteq v) \vee [x; \text{last}([u / v])] \subseteq v$